SUMMER WORK: Calculus AB	Name:
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#### **Preparation for Calculus AB**

Due on the first day of class for homework credit.

1. Read the following lessons from the Calculus AB textbook, then complete the problems listed. Check your solutions to odd problems in the back of the text.

Calculus

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Author: Larson

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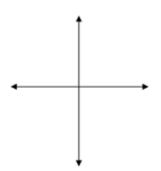
Lesson	Number
P.1	#1-4,9-12,15,19,29,55,57,69,81,83
P.2	#13,19,21b,23,31,35,43,53,57,59,65,69,77
P.3	#1,7,9,17,19,21,25,31,33,35-37,39,41,43,47-52all, 55,57,61,63,65,67,69,71,73,77,78,84,93
P.4	None
Problem Solving, p.39	#3,5,7

2. Complete the attached worksheets and review the topics as needed.

### **Functions**

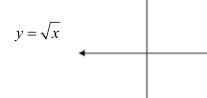
Sketch each of the following functions and state their <u>domain</u> and <u>range</u>. Sketch any <u>asymptotes</u>. You should have these functions and their characteristics memorized.

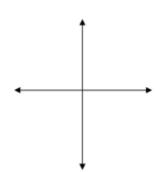
$$y = x$$



$$y = |x|$$

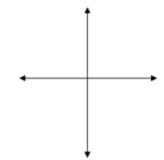
$$y = x^2$$





$$y = x^3$$

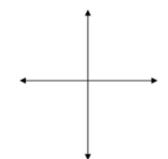
$$y = \sqrt[3]{x}$$

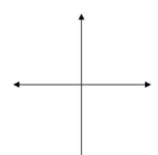


$$y = \frac{1}{x}$$

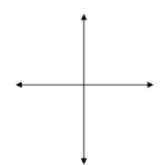


$$y = e^x$$



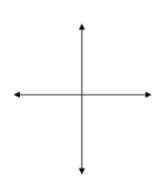


$$y = \ln(x)$$



$$y = \sin(x)$$

$$y = \arcsin(x)$$

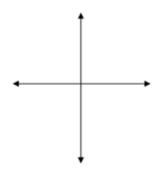


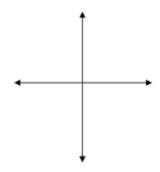
$$y = \cos(x)$$

$$y = \arccos(x)$$

$$y = \tan(x)$$

$$x^2 + y^2 = r^2$$





# **Trig Ratios for Special Angles**

1. Fill in <u>and memorize</u> the values in the following table. You should be able to come up with these values without having to draw the unit circle each time.

Angle	Angle (radians)		cos(x)	tan(x)
(degree)		sin(x)		
0				
30				
45				
60				
90				

2. Find exact values for the following trig ratios:

- 1) Give an exact value for  $\cos \left( \frac{11\pi}{6} \right)$
- 2) Give an exact value for  $\sin \left( \frac{7\pi}{6} \right)$
- 3) Give an exact value for  $\tan \left[ \frac{3\pi}{4} \right]$
- 4) Give an exact value for  $\sin \left[ -\frac{3\pi}{4} \right]$
- 5) Give an exact value for  $\sin \left( \frac{5\pi}{3} \right)$ .
- 6) Give an exact value for  $\cos \left( \frac{7\pi}{3} \right)$
- 7) Give an exact value for  $\sin \left( \frac{17\pi}{6} \right)$
- 8) Give an exact value for  $\tan \left(\frac{18\pi}{6}\right)$

## **Trigonometric Identities**

#### **Pythagorean Identities**

$$\sin^2 x + \cos^2 x = 1$$
  $\tan^2 x + 1 = \sec^2 x$   $1 + \cot^2 x = \csc^2 x$ 

$$\tan^2 x + 1 = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

#### **Examples:**

**1.** Simplify the expression.

$$\cos t + \tan t \sin t$$

**2.** Simplify the expression.

$$\frac{\sin x}{\cos x} + \frac{\cos x}{1 + \sin x}$$

$$\frac{\sec^2 x - 1}{\sec^2 x}$$

**3.** Simplify the expression.

$$\frac{\sec^2 x - 1}{\sec^2 x}$$

## **Properties of Logarithms**

$$\log_b(xy) = \log_b x + \log_b y$$

$$\log_b \left(\frac{x}{y}\right) = \log_b x - \log_b y$$

$$\log_b x^n = n \log_b x$$

## **Examples:**

$$\log\left(\frac{x^2(x-1)^3}{2-x}\right)$$

**1.** Expand the expression.

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$$\frac{1}{2} (3 \ln (x+1) + \ln 5 - 2 \ln x)$$
.

**2.** Condense the expression:

**Simplifying Rational Expressions-** Perform the operation and simplify the following.

a.) 
$$(2x)^4$$

**b.)** 
$$\frac{t}{t^{\frac{1}{3}}}$$

c.) 
$$\frac{3}{x-1} + \frac{x}{x+2}$$
 (need a common denominator)

$$\frac{1}{x^2 - 1} - \frac{2}{(x+1)^2}$$
 (find least common denominator)

$$\frac{\frac{1}{a-h} - \frac{1}{a}}{h}$$
 e.)  $h$  (first, simplify the numerator into one fraction)

$$\frac{\frac{x}{y} - \frac{y}{x}}{\frac{1}{x^2} - \frac{1}{y^2}}$$
 **f.)**

g.) 
$$\frac{\left(1+x^2\right)^{1/2}-x^2\left(1+x^2\right)^{-1/2}}{1+x^2}$$
 (factor out the common factor)

$$\frac{(x-h)^3 - 7(x+h) - (x^3 - 7x)}{h}$$

i.) 
$$\frac{1}{\sqrt{x+1}}$$
 (rationalize the denominator)

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j.) 
$$\frac{\sqrt{r} + \sqrt{2}}{5}$$
 (rationalize the numerator)